

1. Match each function to one of the given graphs, and to one of the given contour diagrams. The plots are given in a separate handout.

$f(x, y)$	Graph	Contour Diagram
$x^2 + \left(\frac{3y}{2}\right)^2$		
$x^2 - y^2$		
$\frac{x}{2} + y$		
$-x + y$		
$\sin(\pi(x - y))$		
xy		
$\sqrt{x^2 + \left(\frac{3y}{2}\right)^2}$		
$x + 2y^2$		

2. (a) Find the equation of the plane that contains the points $(1, 0, 0)$, $(0, -3, 0)$, and $(0, 0, 4)$.
 (b) Find the equation of a sphere centered at $(1, 2, 3)$ that is tangent to the yz -plane.
3. (a) Consider the function

$$f(x, y) = y^2 - \sin(x - y) - 3.$$

Find a function $g(x, y, z)$ such that the graph of f is the level surface $g(x, y, z) = 2$.

- (b) For each of the following functions, determine if the level surface $g(x, y, z) = 1$ can be expressed as the graph of a function $f(x, y)$. If it is not possible, explain why not. If it is possible, find the function $f(x, y)$.
- $g(x, y, z) = x^2 + 2y^2 - z^2$
 - $g(x, y, z) = -x - y + 3z + 8$
 - $g(x, y, z) = e^{x+y+z}$

4. For each of the following, find the indicated partial derivative.

(a) $f(x, y) = xy - 3 \sin x$, $f_x(x, y) =$

(b) $g(x, y) = e^{x-y}$, $f_y(x, y) =$

(c) $h(s, t) = \sqrt{s^2 + st + t^2}$, $\frac{\partial h}{\partial s} =$

(d) $f(x, y) = \ln(x^2 + 2y)$, $f_y(x, y) =$

(e) $P = bL^\alpha K^{1-\alpha}$, $\frac{\partial P}{\partial K} =$

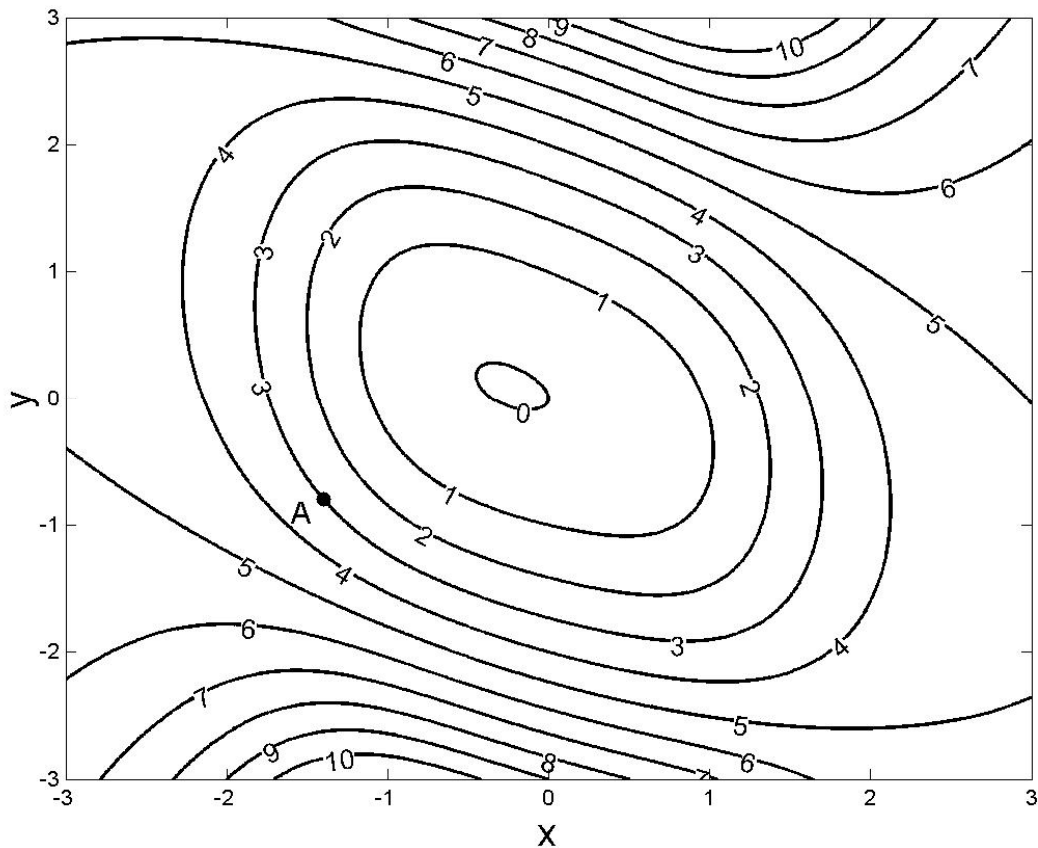
5. Let

$$f(x, y) = (y^2 + 2 + \sin y)x.$$

(a) Find the equation of the plane that is tangent to the graph of f at the point $(3, 0)$.

(b) Use the local linearization of f near $(3, 0)$ to estimate $f(3.2, 0.1)$

6. The following is the contour diagram for a function $f(x, y)$.



Consider the tangent plane to the graph of f at the point labeled A .

(a) In the plot above, sketch the contour diagram of this tangent plane.

(b) Describe and explain your answer to part (a). That is, describe the contours lines, and explain how you know how the curves are shaped and oriented.